## MACM 202 Assignment 2, Spring 2004

This assignment is worth 10% of your grade. It is due Thursday February 5th at 10am. A late penalty of 20% will apply for each day late. Do each question in a separate Maple worksheet and hand in a printout of each worksheet.

Question 1 (10 marks) Locate, using any method, a stable 3-cycle in the logistic map f(x) = ax(1-x). Determine the range end points  $a_L$  and  $a_R$  to 10 decimal digits of precision such that for  $a_L < a < a_R$  the 3-cycle is stable.

Question 2 (40 marks) For the period doubling bifurcations in the logistic map f(x) = ax(1-x) that begin at a=3 compute as many of the period doubling bifurcation points as you can. Estimate the value of Feigenbaum's constant from the values you obtain.

Question 3 (20 marks) Design a boolean network with four nodes which counts in binary from 0 to 15 and then cycles. You may use more than four nodes if you wish but you must identify the four nodes which form the counter. Run your network using the run procedure in the networks worksheet under the assignment lab directory and show the output.

Question 4 (20 marks) Consider a circular boolean network of  $n \geq 3$  nodes numbered 1, 2, ..., n, i.e. each node has one input. Suppose three of the nodes, say nodes 1, s, t where  $1 < s < t \leq n$  apply the "Inverse" rule and the remaining n-3 nodes apply the "Identity" rule. For "sufficiently many" values of (n, s, t) compute the length of the cycle resulting from the initial state [0, 0, ..., 0]. Use the run2cycle procedure in the networks worksheet. Study the data that you obtain and come up with a general rule, for the length of the cycle as a function of (n, s, t). Now verify your rule by running "sufficiently many" values for n, s, t.

Question 5 (10 marks) Write a Maple procedure called ISPRIME which on input of an integer n outputs true if n is prime and false otherwise. This is a simple programming exercise to help you learn to program in Maple. You should do this before Question 2. Use the simple method trial division, i.e. test if n is divisible by  $2, 3, 5, 7, 9, 11, 13, 15, ..., \lfloor \sqrt{n} \rfloor$ . Use the Maple command irem for integer division. Test your code on all odd numbers between 950 and 1000. Use the isprime command to check your answers.