

# MATH 340 Assignment 8, Fall 2007

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This assignment is due Monday December 3rd at the beginning of class.  
For problems requiring Maple please submit a printout of a Maple worksheet.  
Late penalty:  $-20\%$  for up to 24 hours late. Zero after that.

## Section 2.12: Isomorphisms Between (finite) Fields

Exercises 1, 6(i) and prove Lemma 2.12.1 part (ii).

For exercise 1, factor the polynomial  $f(x) = x^3 + x + 1$  over  $F$  and over  $G$ .

## Section 2.14: Error Correcting Codes

Exercises 1, 4, 6, 8, 10.

Use Maple to do the arithmetic in exercise 8.

## Section 3.1: Basic Properties (of Groups)

Exercises 1, 5, 7(iii), 8, 9, 12, 18.

Also, find the isomorphism between the group  $\mathbb{Z}_4(+)$  and the group  $Q(\times)$  where

$$Q = \{1, -1, i, -i\} \text{ and } i^2 = -1.$$

For exercise 18, determine the order of each element of  $D_3$ .