

```

> a := 31;
a := 31
(1)

> b := 21;
b := 21
(2)

> 1/b mod a;
3
(3)

> igcd(a,b);
1
(4)

> g := igcdex(a,b,'s','t');
g := 1
(5)

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```

> s,t;
-2, 3
(6)

> s*a+t*b=g;
1 = 1
(7)

> t;
3
(8)

> a-t;
28
(9)

In Q[x]
> a := x^3-3;
a :=  $x^3 - 3$ 
(10)

> b := x^2+3*x+3;
b :=  $x^2 + 3x + 3$ 
(11)

> gcd(a,b);
1
(12)

> g := gcdex(a,b,x,'s','t');
g := 1
(13)

> s,t;
 $-\frac{1}{3} - \frac{x}{6}, -\frac{1}{6}x + \frac{1}{6}x^2$ 
(14)

> expand(s*a+t*b);
1
(15)

In Z5[x]
> a mod 5;
x^3 + 2
(16)

> b;
x^2 + 3x + 3
(17)

> Gcd(a,b) mod 5;
1
(18)

> g := Gcdex(a,b,x,'s','t') mod 5;
g := 1
(19)

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```

> s,t;

$$4x + 3, x^2 + 4x \quad (20)$$

> Expand(s*a+t*b) mod 5;

$$1 \quad (21)$$

> a,b;

$$x^3 - 3, x^2 + 3x + 3 \quad (22)$$

> q := quo(a,b,x,'r');

$$q := x - 3 \quad (23)$$

> r;

$$6x + 6 \quad (24)$$

> expand(a-b*q-r);

$$0 \quad (25)$$

> q := Quo(a,b,x,'r') mod 5;

$$q := x + 2 \quad (26)$$

> r;

$$x + 1 \quad (27)$$

> Expand(a-b*q-r) mod 5;

$$0 \quad (28)$$

> a;

$$x^3 - 3 \quad (29)$$

> factor(a);

$$x^3 - 3 \quad (30)$$

> Factor(a) mod 5; # factor a over Z5

$$(x + 3)(x^2 + 2x + 4) \quad (31)$$

> factor(a) mod 5; # factor a over Q

$$x^3 + 2 \quad (32)$$

> b := factor(a);

$$b := x^3 - 3 \quad (33)$$

> b mod 5;

$$x^3 + 2 \quad (34)$$


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igcd, irem, iquo, igcdex, ifactor, ilcm for Z
 expand,gcd,rem,quo,gcdex,factor,lcm for Q[x] Q(y1,...yn)[x] over Q characteristic 0
 Expand,Gcd,Rem,Quo,Gcdex,Factor,Lcm for Zp[x] and Zp(y1,...,yn)[x] characteristic p